Appendix 11 Iñupiatun Kisitchiñiq The Iñupiaq Counting System

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The Iñupiat have traditionally used a base-20-sub-base-5 counting system, technically known as a "pentavigesimal system." This indicates that counting is based on groups of five "units," which are, in turn, combined into larger groups composed of four "sets of five." In short, this means that the overarching structure of the system is based on "scores" (or "twenties"). As Iñupiaq numbers become progressively greater, the regroupings by fives and by fours alternate. This characteristic produces a two-dimensional system with a number grid instead of a one-dimensional number line.

The decimal system is handy because the fingers can be used as counters. The Iñupiag base-20 system clearly extends this notion to the toes as well. The Iñupiat counted on one limb at a time, so there were four groups of five, hence the sub-base-5 and the two-dimensional system. The human body may be considered the living model of the earliest abacus or counting board. Even the prototype of the Babylonian base-60 counting system used points on the body to keep track of numbers. The majority of human counting systems are body-based. Some of the Iñupiaq number words clearly reflect their corporal origins. Tallimat, the word for five, for example, is related to the Iñupiaq word taliq, meaning "arm." The word for ten, qulit, means something like "top," suggesting that it refers to both of the arms on the top half of the body. The word for eleven in most Inuit-speaking communities, including some Iñupiaq-speaking communities, means "it goes down," an indication that one is now counting on the toes. Further evidence is found in the word akimiaq, Iñupiaq for fifteen, which means something like "it goes across," implying that counting will now cross over and continue on the other foot.

The connection to the human body is most apparent in the Inuit words used for twenty. Throughout the entire Inuit-speaking world, there is a clear human association. Most Inuit dialects use the same word for "person" as for "twenty." The Iñupiaq word for twenty, iñuiññaq, is a word denoting a "complete person." Inuktitut dialects spoken in Eastern Canada use the word avatit, signifying "all the extremities" of the body. Some have proposed that even the Iñupiaq word atausiq for "one" is probably also derived from a reference to the human body. Atausiq (or some close cognate variation, such as atauceq) is used almost universally where an Inuit dialect is spoken.

One special feature of the Iñupiaq counting system

is the postbase -**ġutaiḷaq**, which anticipates any number (except **tallimat**) and regroups a preceding place value. This postbase suggests that a number is one less than the word stem to which it is attached.

Counting (and numbers) play differing roles, depending on the culture. How extensive the counting system must be is determined by what is counted as well as by how important it is to quantify certain objects. In some cultures, there may be no real need to count higher than fifty or a hundred. In other cultures, it is important to account for very large quantities of some things, so the number system will extend to higher numbers. Until relatively recently, there was rarely a need for Iñupiat to count much above 400. However, when reindeer herding was introduced, the herders sometimes needed much higher numbers to account for each reindeer in a large herd. More recently still, youth in the village of Kaktovik developed an elegant notation system to represent their numbers in written form. Almost immediately, people recognized that the numerals had several advantages over the Arabic numerals when carrying out arithmetic operations. Consequently, the Iñupiaq counting system began to be used in schools for teaching math—with dramatic results. Both reindeer herding and the school math setting introduced new cultural demands, requiring extension of the traditional counting system.

Counting has played many roles in traditional Iñupiaq culture. One of the major roles has been managing a family's yearly requirements for food, clothing, and fuel. The Arctic is very unforgiving and is among the harshest environments on earth. Until recently, with the growth of the cash economy introduced after contact with Western culture, Native families could not survive unless they could manage their resources with foresight and prudence. Accurate counting could be a matter of life or death. It served to ensure that stores of fish, meat, and animal fat or oil were sufficient to sustain the entire family through a long winter.

The number of fish a family held in storage would often be much higher than 400, but it was not necessary to count fish individually. It was the mass, not the number, of fish that was important to a family's survival. A fish rack could hold many more small fish than large fish. Therefore, the fish rack often served as the unit of measure for fish. Larger animals, on the other hand, were counted individually. Skins and pelts that could be used for making clothing, boats, or even shelter were bundled together; the skins of larger animals were bundled in groups of five, and those from smaller animals were fastened together in bundles of twenty. The wife and mother in any Eskimo household knew how many bundles were required for a particular purpose, such as sewing a parka.

Counting was also essential in traditional barter and trade. Arctic peoples from as far away as Siberia regularly attended the annual trade fairs held until early in the twentieth century. There they could trade their own local goods for useful and necessary articles from other regions in order to supplement the products of their own labor, hunting, and gathering.

As mentioned above, the Iñupiaq counting system is a two-dimensional system. By contrast, the decimal system is linear, based only on powers of ten. Ten units (or ones) become 10; ten tens make 100; ten hundreds are 1,000; ten thousands give us 10,000, etc. In the Iñupiaq counting system, five ones (or \s\) are 5 (\subseteq\)), four fives render 20 (\subsete\) δ), five score (twenties) becomes 100 (\subsete\) δ), four hundreds yield 400 (\subsete\) δ δ), five four-hundreds produce 2,000 (\subsete\) δ), and four two-thousands are 8,000 (\subsete\), δ δ δ). Table 1 shows the Kaktovik Iñupiaq numerals used for notation of Iñupiaq numbers.

When naming larger numbers in Iñupiaq, as in most languages, one begins by stating the term that expresses the largest place value. Next, one states the term for the

second-largest place value, continuing until the lowest place value is reached and spoken. The speaker simply skips places that are empty of value (i.e., have a zero value). In Iñupiaq, when no places are empty, the speaker will alternate between place values that are five times the next lowest place value and those that are four times the next lowest place value. The system is a base-20 system precisely because the place values alternate between factors of five and of four times the preceding place value; five times four is twenty. This produces a two-dimensional system. Horizontally the oral system is theoretically infinite, but vertically spoken numbers are limited to two places: the basic place-value units and five times the basic place-value units.

Table 1. Kaktovik Iñupiag numerals.

8	\	V	λ	W		
_	7	∇	Й	W		
>	7	\searrow	$\sqrt{\chi}$	\triangleright		
*	7	₹	K	\mathbf{k}		
(Twenty is written as \dot \dot)						

Table 2. Place values in Arabic and Kaktovik numerals.

1,000,000	50,000 7,~ 8 8	2,500 \(\tag{8}	125	6.25 7.	.3125
200,000	10,000	500 \~8	25	1.25	.0625
40,000 A -,888	2,000 C ~ v v	100 E ~ 8	5 G	.25 I	.0125 K
8,000 B \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	400 D \	20 F \ \ \ \ \	1 H \	.05 J	.0025 L .8\
1,600 W v v	М д 80	4 W	.2 .W	.01	.0005
320 ₹8	16 *	.8 . *	.04 .ŏ ₹	.002 .∀∀₹	.0001 .v v <

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However, the traditional oral system can easily be expanded beyond the two spoken vertical place values. For specific purposes, some Inuit communities expand the simple base-5 system higher. One example is the special base-5 counting system used in Greenland for counting and binding birds together. When hunting from a kayak, the hunter uses the weight of the birds to maintain stability and balance the load. However, all the places in the oral system can, in theory, be extended infinitely higher and lower. The base-5 axis can be extended one or more places higher or lower in order to make calculation simpler when using the penta-vigesimal system to solve math problems. Table 2 shows the place values in both Arabic and Kaktovik numerals of the various places when the spoken system is expanded vertically. The band of value places shown in gray indicates places used in the spoken counting system. The capitalized letters, shown in the center, indicate the spoken order of the corresponding oral number words, beginning with "A."

Note that when moving up or down in Table 2, the place values increase or decrease by a factor of five. When moving left or right, the place values increase or decrease by a factor of twenty. When moving diagonally down and left or up and right, the place values increase or decrease by a factor of four. When moving diagonally up and left or down and right, the place values increase or decrease by a factor of one hundred. Also notice the Kaktovik numeral in each horizontal row is a numeral, or a pair of them, which remains constant across the row, only changing the place value where those numerals occur, as they increase or decrease by a factor of twenty. The vertical double line separates whole numbers from vigesimal fractions.

The oral Iñupiaq counting system uses tallimat, with or without a postbase (e.g., tallimat, tallimakipiaq, tallimagliaq, etc.), to indicate value five times that of the next-lower place value. For example, the value is 5 when the next lower place value is 1; it is 100 when the lower place value is 20; and 2,000 when the lower place value is 400, etc. The oral system uses qulit, qulikipiaq, quliagliaq, etc. to show value twice five times (or ten times) the value of the next lower place value; it is, for example, 10 when the lower place value is 1; 200 when the lower place value is 20; 4,000 when the lower place value is 400, etc. In the same way, it uses akimiaq, with or without a postbase (e.g., akimiaq, akimiakipiaq, akimiagliaq, etc.) to indicate value thrice five times (or fifteen times) the value of the basic unit value of the next lower place. For example, it is 15 when the lower place value is 1; 300 when the lower place value is 20; 6,000 when the lower place value is 400, etc. By contrast, malguk, pinasut, and sisamat are used in the lower sector, or place, with or without a postbase, to indicate respectively a value two, three, or four times the value of the basic value unit in that lower sector, or place.

In order to represent this oral system simply with symbols, every Kaktovik numeral contains information about two places: a lower place value and an upper place value (whose value is five times the value of the lower place). In both sectors, a single straight stroke is used to represent one unit of value; two strokes represent two units of value; three strokes represent three units of value. This means that mathematically both λ and \sim represent one value unit; both λ and \sim represent two value units; both λ and \sim represent three value units. The difference is that the stroke pattern used in the lower sector is rotated ninety degrees to the left and elevated when written to show the value in the upper sector, or place.

The elevation shows that the stroke pattern occupies a different place and has a higher place value. The rotation and elevation together remind us that the rotated form has a value five times greater than in the place below. They also remind us that **qulit** and **akimiaq** are the appropriate oral stems, rather than **malġuk** and **piŋasut**. When both sectors (or places) of one Kaktovik numeral contain strokes indicating value, the upper and lower strokes are graphically connected. If there are no strokes in one of the places (or sectors), that sector without any strokes is deemed empty (as though it contained a zero). **Suitchuq**, the equivalent of zero, is only needed when there is absence of value in both the upper and lower sectors. **Suitchuq** is a dual place holder, normally signifying that both the lower sector, or place, it occupies and the upper sector, or place, are empty.

Table 3 shows the place values for a large whole number written with Arabic numerals and occupying five places in the decimal system. It also shows the equivalent of the same number using only four Kaktovik numerals yet occupying eight places. The table also indicates (in parentheses) how that place value is determined as a multiple of the place value of the preceding place in the system. Note the linear nature of the decimal system, which has only one base in contrast to the penta-vigesimal system, which has both a base and sub-base, and places are arranged both vertically and horizontally.

When written with the Kaktovik Iñupiaq numerals, the equivalent of the number 97,531, for example, occupies eight places in the Iñupiaq place-value system, whereas it occupies only five places in the decimal system (see Table 4). Nevertheless, only four numerals are required to express 97,531 in Kaktovik numerals: , , , , , Fewer numerals are needed because each Kaktovik numeral expresses quantities for two places in the Iñupiaq place-value system, as shown in Table 4 below. Notice the column of Kaktovik numerals highlighted in gray; also notice how those Kaktovik numerals, shown in the third column, are composed of the two stroke patterns in the fourth column. (Forms in parentheses are non-rotated forms.)

Arabic Numeral Place Value

Table 3. Place values for a large whole number.

1,000 10 1 100 **Decimal** thousands hundreds tens ones **Place Values** $[10^3]$ $[10^{1}]$ $[10^{0}]$ $[10^{2}]$ Kaktovik Numeral Place Value ~,<u>v v v</u> 788 Iñupiaq (5 X 1)(5 X 8,000)(5 X 400)(5 X 20)**Upper-sector** fives forty-thousands two-thousands hundreds **Place Values** 40,000 2,000 100 5 /* x x x / g g / g 1 Iñupiaq (4 X 2,000) (4 X 100) (4 X 5)Lower-sector eight-thousands four-hundreds scores ones **Place Values** 8,000 400 20 $[20^{0}]$ $[20^3]$ $[20^2]$ $[20^{1}]$

Table 4. The Decimal System and the Iñupiag System.

97,531 in the Decimal System		97,531 in the Decimal System $\nabla, \kappa \uparrow \uparrow = 97,531$ in the Iñupiaq System		ñupiaq System	
		>	> _(V)	2	forty-thousands
		V	V	2	eight-thousands
			(8)	0	two-thousands
9	ten-thousands	N	Ν	3	four-hundreds
7	thousands	*	> (N)	3	hundreds
5	hundreds	\	١	1	score
3	tens	>	> _(V)	2	fives
1	ones	\	١	1	ones

The second and the last columns in Table 4 indicate the place values of each place in the respective systems. The first and fifth columns specify, in Arabic numerals, how many multiples of each place value there are. The fourth column gives the stroke pattern of the forms used in a Kaktovik numeral to indicate the same value that is shown in the fifth column. When the form of the basic stroke pattern has been rotated and elevated, the non-rotated form is given in parentheses so that its relationship to the Arabic numerals of the fifth column is clearer. Finally, in the third column, the

reader sees the complete Kaktovik numeral that is composed from two elements in the fourth column.

Since contact with the West began, Inuit-speaking communities have experienced strong interference and pressure from the English, French, Russian, and Danish counting systems. For the typical person who knows the decimal system better than the local Inuit penta-vigesimal system, confusion tends to set in as the numbers get higher. The confusion arises from the fact that in English the word "forty" is related to the word "four," whereas, for example,

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the Iñupiag word equivalent to eighty is derived from the Iñupiaq word for four. As Inuit began to be educated in the decimal system, they easily equated or confused their word for eighty with the English word for forty, unless they were very familiar with their traditional system. Also, the English word "thirty" is related to the words "third" and "three," whereas in Iñupiag, as in other Inuit dialects, the word equivalent to sixty is derived from the Iñupiag word for three. Therefore, educated Inuit also confused their word for sixty with the decimal number "thirty." This has resulted in a tendency, during the post-contact period, for numbers thirty and above to fall into disuse. In some communities, the traditional Inuit sub-base-5 structure has even mutated into a sub-base-10 system, thus making the local traditional counting system more compatible with the decimal system. This tendency has been particularly marked in Eastern Canada. However, this change obscures some of the genius and simplified calculation benefits of the traditional Inuit system.

The table on the following pages is intended to help Iñupiaq learners and speakers become more familiar with the Iñupiaq counting system. In each column of the table, the Kaktovik numeral, the Iñupiaq number name, and the decimal equivalent are given, in that order. The table is divided into groups of five to visually distinguish each group of five. The Iñupiag for every whole number up to the equivalent of 400 is given, as well as the equivalent of zero. After 400, larger Iñupiag number words for multiples of 400, 8,000, 160,000, and 3,200,000 are shown, from which the reader can extrapolate the remaining Iñupiag numbers and Kaktovik numeral counterparts almost up to 2,048,000,000,000,000. Compare the Kaktovik numerals to the Iñupiag number words. Notice how, for each Kaktovik numeral, both place values are generally read separately. Exceptions such as itchaksrat exist, not unlike "eleven" in the English system. Also pay attention to numbers ending in -gutailaq, just above lines separating the cycles or groups of five. These numbers cause some difficulty to those unfamiliar with the Iñupiag counting system. Although this feature may seem a nuisance at first, it is, nevertheless, an excellent linguistic aid for students learning to do complex computation quickly on a penta-vigesimal Iñupiaq abacus or counting board.

Iñupiaq Counting System with Kaktovik Numerals (first column) and Arabic Numeral Equivalents (third column)

suitchuq (*see note)	0
atausiq	1
malġuk	2
piŋasut	3
sisamat	4
tallimat	5
itchaksrat	6
tallimat malġuk	7
tallimat piŋasut	8
quliŋŋuġutaiḷaq	9
qulit	10
qulit atausiq	11
qulit malġuk	12
qulit piŋasut	13
akimiaġutaiḷaq	14
akimiaq	15
akimiaq atausiq	16
	17
	18
iñuiññaġutaiḷaq	19
	atausiq malġuk piŋasut sisamat tallimat itchaksrat tallimat malġuk tallimat piŋasut quliŋŋuġutaiḷaq qulit qulit atausiq qulit malġuk qulit piŋasut akimiaġutaiḷaq akimiaq akimiaq

	<u> </u>	
١ ४	iñuiññaq	20
١١	iñuiññaq atausiq	21
۱۷	iñuiññaq malġuk	22
١٧	iñuiññaq piŋasut	23
١W	iñuiññaq sisamat	24
\-	iñuiññaq tallimat	25
17	iñuiññaq itchaksrat	26
١٧	iñuiññaq tallimat malġuk	27
١٨	iñuiññaq tallimat piŋasut	28
١₩	iñuiññaq quliŋŋuġutaiḷaq	29
\>	iñuiññaq qulit	30
71	iñuiññaq qulit atausiq	31
√₹	iñuiññaq qulit malġuk	32
۱ గ	iñuiññaq qulit piŋasut	33
\₩	iñuiññaq akimiaġutaiḷaq	34
\>	iñuiññaq akimiaq	35
۱٤	iñuiññaq akimiaq atausiq	36
١₹	iñuiññaq akimiaq malġuk	37
١ గ	iñuiññaq akimiaq piŋasut	38
\₩	malġukipiaġutaiḷaq	39
	C 41: ((1 · · · 1 · · · 1 · · · · · · · · · ·	_

	<u> </u>	
V &	malġukipiak	40
٧١	malġukipiaq atausiq	41
٧٧	malġukipiaq malġuk	42
٧٨	malġukipiaq piŋasut	43
VW	malġukipiaq sisamat	44
v-	malġukipiaq tallimat	45
٧٢	malġukipiaq itchaksrat	46
٧V	malġukipiaq tallimat malġuk	47
٧Й	malġukipiaq tallimat piŋasut	48
∨ ₩	malġukipiaq quliŋŋuġutaiḷaq	49
ν>	malġukipiaq qulit	50
7 _V	malġukipiaq qulit atausiq	51
√₹	malġukipiaq qulit malġuk	52
$\sqrt{\chi}$	malġukipiaq qulit piŋasut	53
$\vee \widetilde{\mathbb{W}}$	malġukipiaq akimiaġutaiḷaq	54
√ ≤	malġukipiaq akimiaq	55
√٢	malġukipiaq akimiaq atausiq	56
v₹	malġukipiaq akimiaq malġuk	57
V₩	malġukipiaq akimiaq piŋasut	58
∨₩	piŋasukipiaġutaiḷaq	59
ordinal t	o show order as when counting or to exp	ress

*"Suitchuq" is a cardinal used to express the value of nothing or zero; "kisitchisagvik" is used as an ordinal to show order, as when counting or to express the power of zero.

Иα	piŋasukipiaq	60
м∖	piŋasukipiaq atausiq	61
NV	piŋasukipiaq malġuk	62
NΝ	piŋasukipiaq piŋasut	63
ΝW	piŋasukipiaq sisamat	64
ν -	piŋasukipiaq tallimat	65
NΓ	piŋasukipiaq itchaksrat	66
ηV	piŋasukipiaq tallimat malġuk	67
ηЙ	piŋasukipiaq tallimat piŋasut	68
ΝW	piŋasukipiaq quliŋŋuġutaiḷaq	69
ν>	piŋasukipiaq qulit	70
7 _N	piŋasukipiaq qulit atausiq	71
νŞ	piŋasukipiaq qulit malġuk	72
йи	piŋasukipiaq qulit piŋasut	73
νŵ	piŋasukipiaq akimiaġutaiḷaq	74
η×	piŋasukipiaq akimiaq	75
'nξ	piŋasukipiaq akimiaq atausiq	76
ห⊽ี	piŋasukipiaq akimiaq malġuk	77
ทที	piŋasukipiaq akimiaq piŋasut	78
νŘ	sisamakipiaģutaiļaq	79

Μα	sisamakipiaq	80
w١	sisamakipiaq atausiq	81
WV	sisamakipiaq malġuk	82
wν	sisamakipiaq piŋasut	83
ww	sisamakipiaq sisamat	84
w-	sisamakipiaq tallimat	85
w۲	sisamakipiaq itchaksrat	86
w∇	sisamakipiaq tallimat malġuk	87
wπ	sisamakipiaq tallimat piŋasut	88
ΝW	sisamakipiaq quliŋŋuġutaiḷaq	89
w>	sisamakipiaq qulit	90
٧٢	sisamakipiaq qulit atausiq	91
w₹	sisamakipiaq qulit malġuk	92
wγ	sisamakipiaq qulit piŋasut	93
ww	sisamakipiaq akimiaġutaiļaq	94
w≤	sisamakipiaq akimiaq	95
w₹	sisamakipiaq akimiaq atausiq	96
w₹	sisamakipiaq akimiaq malguk	97
wπ	sisamakipiaq akimiaq piŋasut	98
w₩	tallimakipiaģutaiļaq	99

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- ₈	tallimakipiaq	100
-\	tallimakipiaq atausiq	101
~ _V	tallimakipiaq malġuk	102
- N	tallimakipiaq piŋasut	103
-w	tallimakipiaq sisamat	104
	tallimakipiaq tallimat	105
-7	tallimakipiaq itchaksrat	106
-V	tallimakipiaq tallimat malġuk	107
-₩	tallimakipiaq tallimat piŋasut	108
-₩	tallimakipiaq quliŋŋuġutaiḷaq	109
->	tallimakipiaq qulit	110
->	tallimakipiaq qulit atausiq	111
~>	tallimakipiaq qulit malġuk	112
7	tallimakipiaq qulit piŋasut	113
-₩	tallimakipiaq akimiaģutaiļaq	114
-=	tallimakipiaq akimiaq	115
-5	tallimakipiaq akimiaq atausiq	116
-₹	tallimakipiaq akimiaq malguk	117
-₹	tallimakipiaq akimiaq piŋasut	118
-₩	tallimakipiaq iñuiññaġutaiḷaq	119

78	tallimakipiaq iñuiññaq	120
۲۱	tallimakipiaq iñuiññaq atausiq	121
۲v	tallimakipiaq iñuiññaq malġuk	122
۲n	tallimakipiaq iñuiññaq piŋasut	123
۲w	tallimakipiaq iñuiññaq sisamat	124
7-	tallimakipiaq iñuiññaq tallimat	125
77	tallimakipiaq iñuiññaq itchaksrat	126
77	tallimakipiaq iñuiññaq tallimat malġuk	127
77	tallimakipiaq iñuiññaq tallimat piŋasut	128
۲W	tallimakipiaq iñuiññaq quliŋŋuġutaiḷaq	129
۲>	tallimakipiaq iñuiññaq qulit	130
77	tallimakipiaq iñuiññaq qulit atausiq	131
77	tallimakipiaq iñuiññaq qulit malġuk	132
77	tallimakipiaq iñuiññaq qulit piŋasut	133
マダフ	tallimakipiaq iñuiññaq akimiaġutaiḷaq	134
۲ ×	tallimakipiaq iñuiññaq akimiaq	135
77	tallimakipiaq iñuiññaq akimiaq atausiq	136
77	tallimakipiaq iñuiññaq akimiaq malġuk	137
77	tallimakipiaq iñuiññaq akimiaq piŋasut	138
T \$\vec{v}\$	tallimakipiaq malģukipiaģutaiļaq	139

۷۷	tallimakipiaq malġukipiaq	140
Σ١	tallimakipiaq malġukipiaq atausiq	141
∇V	tallimakipiaq malġukipiaq malġuk	142
٧N	tallimakipiaq malģukipiaq piŋasut	143
∇w	tallimakipiaq malġukipiaq sisamat	144
V-	tallimakipiaq malģukipiaq tallimat	145
77	tallimakipiaq malġukipiaq itchaksrat	146
$\nabla\nabla$	tallimakipiaq malġukipiaq tallimat malġuk	147
$\nabla \nabla$	tallimakipiaq malġukipiaq tallimat piŋasut	148
$\nabla \overline{\mathbf{w}}$	tallimakipiaq malģukipiaq quliŋŋuġutaiļaq	149
√>	tallimakipiaq malġukipiaq qulit	150
77	tallimakipiaq malġukipiaq qulit atausiq	151
$\nabla \nabla$	tallimakipiaq malġukipiaq qulit malġuk	152
77	tallimakipiaq malġukipiaq qulit piŋasut	153
∇₩	tallimakipiaq malġukipiaq akimiaġutaiḷaq	154
√×	tallimakipiaq malġukipiaq akimiaq	155
٢ ٢	tallimakipiaq malgukipiaq akimiaq atausiq	156
√₹	tallimakipiaq malgukipiaq akimiaq malguk	157
ô	tallimakipiaq malgukipiaq akimiaq piŋasut	158
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Пъ	tallimakipiaq piŋasukipiaq	160
П١	tallimakipiaq piŋasukipiaq atausiq	161
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۲>	tallimakipiaq piŋasukipiaq qulit	170
77	tallimakipiaq piŋasukipiaq qulit atausiq	171
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₩₩	qulikipiaq sisamakipiaq akimiaq piŋasut	298
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≤W	akimiakipiaq quliŋŋuġutaiḷaq	309
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₹٧	akimiakipiaq iñuiññaq malġuk	322
۴n	akimiakipiaq iñuiññaq piŋasut	323
۲w	akimiakipiaq iñuiññaq sisamat	324
F-	akimiakipiaq iñuiññaq tallimat	325
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₹5	akimiakipiaq iñuiññaq tallimat malġuk	327
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77	akimiakipiaq iñuiññaq qulit piŋasut	333
₹ %	akimiakipiaq iñuiññaq akimiaġutaiḷaq	334
*	akimiakipiaq iñuiññaq akimiaq	335
77	akimiakipiaq iñuiññaq akimiaq atausiq	336
₹₹	akimiakipiaq iñuiññaq akimiaq malġuk	337
77	akimiakipiaq iñuiññaq akimiaq piŋasut	338
¥ V	akimiakipiaq malġukipiaġutaiļaq	339

₹8	akimiakipiaq malġukipiaq	340
₹١	akimiakipiaq malġukipiaq atausiq	341
₹٧	akimiakipiaq malġukipiaq malġuk	342
₹n	akimiakipiaq malġukipiaq piŋasut	343
₹w	akimiakipiaq malġukipiaq sisamat	344
₹-	akimiakipiaq malġukipiaq tallimat	345
₹٢	akimiakipiaq malġukipiaq itchaksrat	346
₹√	akimiakipiaq malģukipiaq tallimat malģuk	347
₹ñ	akimiakipiaq malġukipiaq tallimat piŋasut	348
₹W	akimiakipiaq malġukipiaq quliŋŋuġutaiḷaq	349
₹>	akimiakipiaq malġukipiaq qulit	350
₹₹	akimiakipiaq malġukipiaq qulit atausiq	351
₹₹	akimiakipiaq malġukipiaq qulit malġuk	352
₹₹	akimiakipiaq malġukipiaq qulit piŋasut	353
₹₩	akimiakipiaq malġukipiaq akimiaġutaiḷaq	354
₹≤	akimiakipiaq malġukipiaq akimiaq	355
₹₹	akimiakipiaq malgukipiaq akimiaq atausiq	356
₹₹	akimiakipiaq malġukipiaq akimiaq malġuk	357
₹₹	akimiakipiaq malgukipiaq akimiaq pinasut	358
₹₹	akimiakipiaq piŋasukipiaġutaiḷaq	359

₹8	akimiakipiaq piŋasukipiaq	360
ለ	akimiakipiaq piŋasukipiaq atausiq	361
ЙV	akimiakipiaq piŋasukipiaq malġuk	362
ที่ท	akimiakipiaq piŋasukipiaq piŋasut	363
พีพ	akimiakipiaq piŋasukipiaq sisamat	364
₹-	akimiakipiaq piŋasukipiaq tallimat	365
77	akimiakipiaq piŋasukipiaq itchaksrat	366
ቑዾ	akimiakipiaq piŋasukipiaq tallimat malġuk	367
ЙΨ	akimiakipiaq piŋasukipiaq tallimat piŋasut	368
МW	akimiakipiaq piŋasukipiaq quliŋŋuġutailaq	369
₹>	akimiakipiaq piŋasukipiaq qulit	370
77	akimiakipiaq piŋasukipiaq qulit atausiq	371
₹₹	akimiakipiaq piŋasukipiaq qulit malġuk	372
N M	akimiakipiaq piŋasukipiaq qulit piŋasut	373
₹\$	akimiakipiaq piŋasukipiaq akimiaġutaiḷaq	374
₹≍	akimiakipiaq piŋasukipiaq akimiaq	375
77	akimiakipiaq piŋasukipiaq akimiaq atausiq	376
₹₹	akimiakipiaq piŋasukipiaq akimiaq malġuk	377
КK	akimiakipiaq piŋasukipiaq akimiaq piŋasut	378
₩.	akimiakipiaq sisamakipiaġutaiḷaq	379

₩ 8	akimiakipiaq sisamakipiaq	380
₩\	akimiakipiaq sisamakipiaq atausiq	381
$\tilde{\mathbb{W}}$	akimiakipiaq sisamakipiaq malġuk	382
พีท	akimiakipiaq sisamakipiaq piŋasut	383
₩w	akimiakipiaq sisamakipiaq sisamat	384
₩-	akimiakipiaq sisamakipiaq tallimat	385
ъГ	akimiakipiaq sisamakipiaq itchaksrat	386
₩٧	akimiakipiaq sisamakipiaq tallimat malġuk	387
$\overline{\mathbb{M}}$	akimiakipiaq sisamakipiaq tallimat piŋasut	388
พีพ	akimiakipiaq sisamakipiaq qulinnugutailaq	389
≨>	akimiakipiaq sisamakipiaq qulit	390
₹7	akimiakipiaq sisamakipiaq qulit atausiq	391
₹₹	akimiakipiaq sisamakipiaq qulit malġuk	392
₩.	akimiakipiaq sisamakipiaq qulit piŋasut	393
₩₩	akimiakipiaq sisamakipiaq akimiaģutaiļaq	394
₹×	akimiakipiaq sisamakipiaq akimiaq	395
₩ ₹	akimiakipiaq sisamakipiaq akimiaq atausiq	396
∳₹	akimiakipiaq sisamakipiaq akimiaq malguk	397
₩₩	akimiakipiaq sisamakipiaq akimiaq piŋasut	398
₩₩	iñuiññakipiaġutaiļaq or iļagiññaġutaiļaq	399

/ g g	iñuiññakipiaq (traditional form)	400
	or, in reindeer herding and math, ilagiññaq	
Λαα	malġuagliaq	800
Ияя	piŋasuagliaq	1,200
Мяя	sisamaagliaq	1,600
-88	tallimaagliaq	2,000
788	tallimaagliaq ilagiññaq	2,400
V××	tallimaagliaq malguagliaq	2,800
N88	tallimaagliaq piŋasuagliaq	3,200
พีงง	tallimaagliaq sisamaagliaq	3,600
> 8 8	quliagliaq	4,000
788	quliagliaq iḷagiññaq	4,400
₹ 8 8	quliagliaq malġuagliaq	4,800
₹8 8	quliagliaq piŋasuagliaq	5,200
₩88	quliagliaq sisamaagliaq	5,600
≤ _{8 8}	akimiagliaq	6,000
₹88	akimiagliaq ilagiññaq	6,400
₹88	akimiagliaq malģuagliaq	6,800
₹88	akimiagliaq piŋasuagliaq	7,200
พีซซ	akimiagliaq sisamaagliaq	7,600

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₩₩₩	atausiqpautaiļaq	7,999	
7.888	atausiqpak	8,000	
٧.٧٧	malġuqpak	16,000	
М . 8 8 8	piŋasuqpak	24,000	
M. g g g	sisamaqpak	32,000	
888	tallimaqpak	40,000	
7.888	tallimaqpak atausiqpak	48,000	
√.888	tallimaqpak malġuqpak	56,000	
П. 888	tallimatqak piŋasuqpak	64,000	
พี.ชชช	tallimaqpak sisamaqpak	72,000	
>. 8 8 8	quliqpak	80,000	
7.888	quliqpak atausiqpak	88,000	
₩. 8 8 8	quliqpak malġuqpak	96,000	
<u>~</u> .∀∀∀	quliqpak pinasuqpak	104,000	
พี.ชชช	quliqpak sisamaqpak	112,000	
≤ _. ४४४	akimiaqpak	120,000	
F. 8 8 8	akimiaqpak atausiqpak	128,000	
₹.888	akimiaqpak malġuqpak	136,000	
₹.888	akimiaqpak piŋasuqpak	144,000	
พี.ชชช	akimiaqpak sisamaqpak	152,000	

₩.₩₩	iñuiññaqpautaiḷaq	159,999
7 8 . 8 8 8	iñuiññaqpak	160,000
-8.888	tallimakipiaqpak	800,000
> 2 . 2 2 2	qulikipiaqpak	1,600,000
≥ ^{8,888}	akimiakipiaqpak	2,400,000
₩₩.₩₩	iļagiññaqpautaiļaq	3,199,999
/ ממ'ממ/	iļagiññaqpak	3,200,000
_ 8 8 . 8 8 8	tallimaagliaqpak	16,000,000
> ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~	quliagliaqpak	32,000,000
<pre><pre><pre></pre></pre></pre>	akimiagliaqpak	48,000,000
/.४४४.४४	atausiqpakaippaq	64,000,000
7 2 2 2 2 2 2 7	iñuiññaqpakaippaq	1,280,000,000
> 8.888888	qulikipiaqpakaippaq	12,800,000,000
\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	iļagiññaqpakaippaq	25,600,000,000
\$\$\$.\$\$\$.	atausiqpakpinatchagutai	laq 511,999,999,999
/.888.888.888	atausiqpakpiŋatchaq	512,000,000,000
7 8.8 8 8.8 8 8.8 8	iñuiññaqpakpiŋatchaq	10,240,000,000,000
> 2. 2 2 2 2 2 2 2 2 2	qulikipiaqpakpinatchaq	102,400,000,000,000
/ & & . & & & . & & . & & & & & & & & &	ilagiññaqpakpiŋatchaq	204,800,000,000,000
> 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	quliagliaqpakpinatchaq	2,048,000,000,000,000

In this table, periods are used instead of commas in the Kaktovik numerals.